

# Finding a Green Nudge: An Evolutionary Perspective

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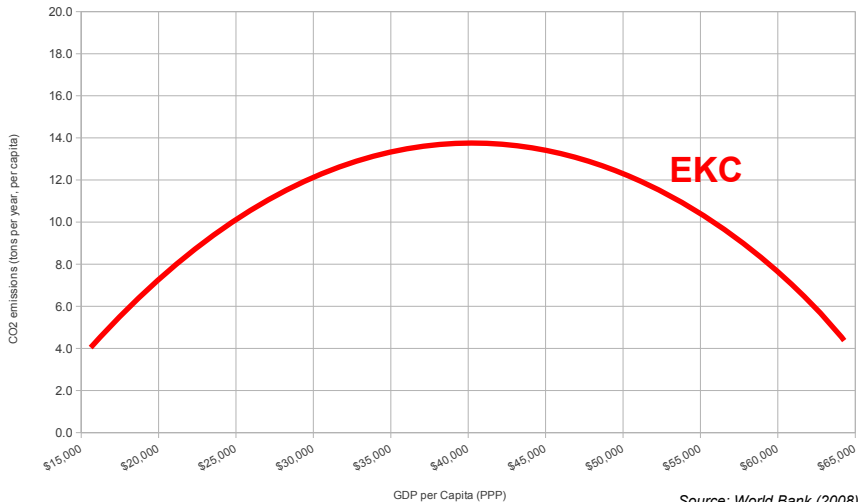
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Columbia University  
April 13th, 2013

# Motivation

General questions which motivate this work:

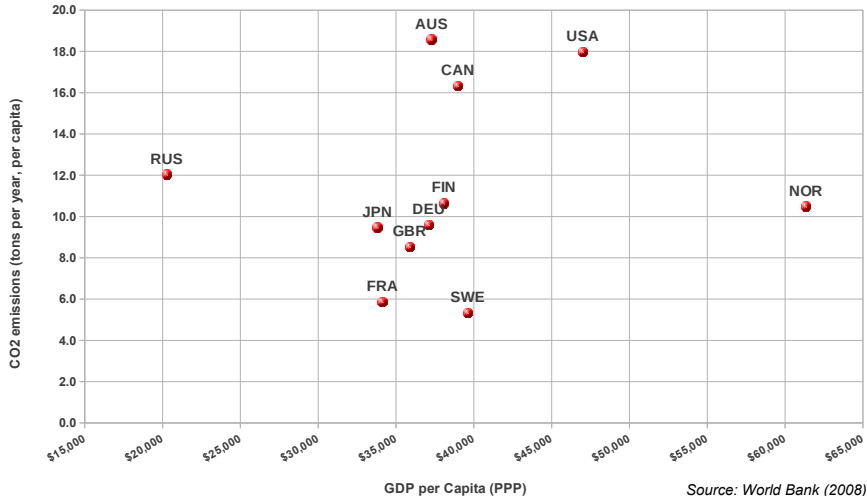
- Is it possible to obtain and sustain a good environment?
- Meaning: Are we able to auto-regulate ourselves and achieve this objective in the long term?
- Why do some countries behave 'green', whereas others behave 'brown'? Are the Environmental Kuznets Curves the (only) explanation?

# Motivation



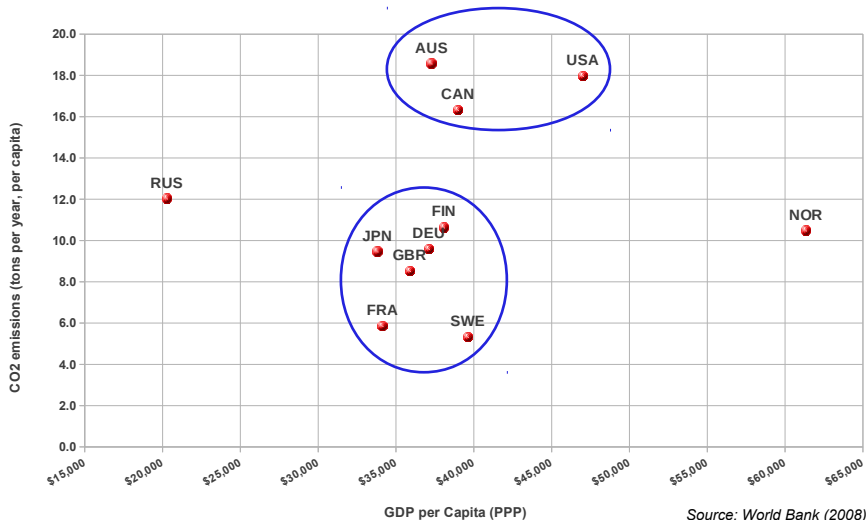
Source: World Bank (2008)

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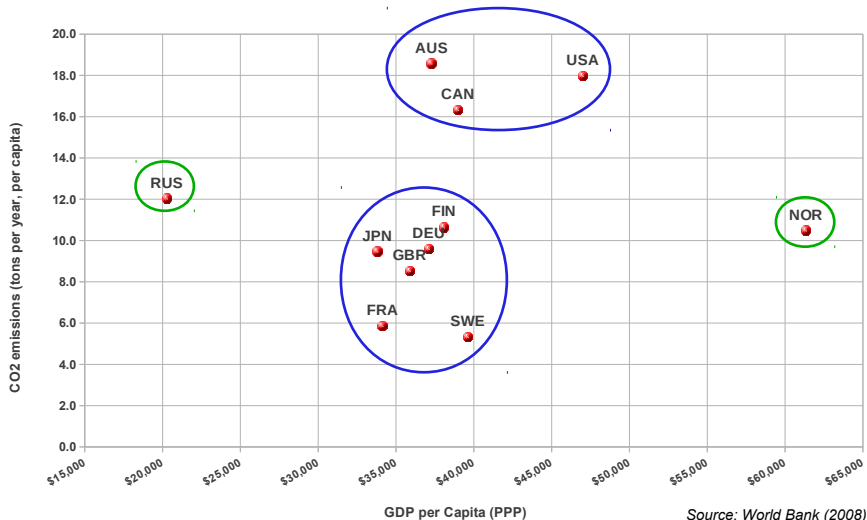
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- Why similar countries (from an economic point of view) like the U.S. and the Nordic countries can behave so differently with respect to the environment?
- It looks like the environmental problem is not (only) a technical one, but a *socio-political* one.

# Motivation

The aim of the present work is:

- To analyse the possibility of having two similar countries ending up in different environmental conditions.
- Try to understand the possible reasons of this phenomenon.
- To find a way of shifting from a brown equilibrium (path) to a green one (maybe through some *tipping points*?<sup>1</sup>).

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<sup>1</sup>Concept from Schelling's book '*Micromotives and Macrobehavior*' (1978) and with '*The Tipping Point*', book by Malcolm Gladwell, 2000.  
Formal definition: Lamberson & Page (2012), '*Tipping Points*'.



## General Framework - The People

A society with **types** of people: Those who are concerned about the environment and those who are not.

- $n \rightarrow 2$  (to keep it simple): The green and brown people.

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<sup>2</sup>As in from Brekke, Kverndokk & Nyborg (2001): '*An economic model of moral motivation*'.

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## General Framework - The People

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- $n \rightarrow 2$  (to keep it simple): The green and brown people.

Green people:

- Their utility will derive not only from consumption.
- But also from 'moral' motivation,<sup>2</sup> coming from:
  - Their contribution to the environment ( $r$ ).
  - Their awareness/worry about the environment ( $p_t$ ).

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## General Framework - The Society

The society is compounded by a **share** of green people ( $q_t$ ) and brown people ( $1 - q_t$ ).

An 'evolving' society.

- The proportion of these people will change in time (as observed in real life).
- As seen in Sethi and Somanathan:<sup>3</sup> It will evolve in favour of those groups getting higher benefits.
- Which is based on replicator dynamics.<sup>4</sup>

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<sup>3</sup>Sethi and Somanathan: 'Evolution of Social Norms' (1996).

<sup>4</sup>Taylor and Jonker: 'Evolutionarily Stable Strategies and Game Dynamics' (1978).

## General Framework - The Goods and Environment

There will be two types of goods in the society:

- A 'brown' good:
  - Which pollutes.
  - And is 'cheap': price = 1.
- A 'green' good:
  - Which does not pollute.
  - But it is more expensive: price =  $1 + \rho$ .

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Pollution level answers a stock equation:

- $\dot{p}_t = -\eta p_t + \gamma d_t$   
( $d_t$ : Total brown product consumption)

## General Framework

A **government** which answers to a simple majority rule:

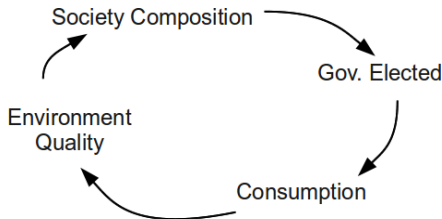
- If  $q_t < 1/2$  a brown government will be elected.
- Otherwise, a green government will be elected.
- A green government will implement a green policy.

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- Otherwise, a green government will be elected.
- A green government will implement a green policy.

The cycle:





# The General Framework

A proportion  $q_t$  of green people and conversely  $(1 - q_t)$  of brown people.

The society can consume two types of goods:

- A green good ( $x_i$ ): which does not pollute, but price =  $1 + \rho$ .
- A brown one ( $y_i$ ): which does pollute, but cheaper: price = 1.

Each agent can consume both:

- Green person:  $\mathbf{x}_G$  green prod +  $\mathbf{y}_G$  brown prod =  $\mathbf{c}_G$  products
- Brown person:  $\mathbf{x}_B$  green prod +  $\mathbf{y}_B$  brown prod =  $\mathbf{c}_B$  products

They have a fixed income  $w$ :

- Budget constraint:  $x_i(1 + \rho) + y_i = w \quad i \in \{G, B\}$

# The People

The difference between green and brown people is:  
Brown people are pure homo-economicus:

$$U_B = u(c_B) \rightarrow c_B = y_B = w$$

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$m(r, p_t)$ : Moral gain coming from:

- $r$ : their **contribution** to the environment  $\equiv$  the **share** of green products bought:  $r = x_G/c_G$ .
- $m_3(p_t)$ : their awareness/worry about the environment.

$m(r, p_t) \rightarrow \leftarrow u(c_G)$ : Trade-off between contributing and the consumption level.

## The green agent's program

Lets recall that  $r = x_G/c_G$

- Amount of green product:  $x_G = r c_G$
- Amount of brown product:  $y_G = (1 - r)c_G$

So the budget constraint becomes:  $(1 + \rho)r c_G + (1 - r)c_G = w$

Giving the quantity of products consumed by the green person:

$$c_G = \frac{w}{(1 + r\rho)} = c_G(r) \quad \rightarrow \quad \underbrace{\frac{\partial c_G}{\partial r}}_{\text{the trade-off of being green}} < 0$$

The more he contributes ( $r \uparrow$ ), the less he consumes ( $c_G \downarrow$ ).

# Moral gain

$$m(r, p_t) = \underbrace{\alpha_1 m_1(r)}_{\text{contribution}} \cdot \underbrace{m_3(p_t)}_{\text{awareness}}$$

## Contribution:

- I feel better when I contribute:  $m_1(r)$  is an increasing function.

## Awareness:

- The idea: The worse the environment, the **worrier** or more **aware** people get.
  - $m_3(p_t)$  is an increasing function of  $p_t$ .
  - For simplicity:  $m_3(p_t) = \Omega_3 p_t$
  - $\Omega_3 > 0$  is the perception bias of the pollution level.

$\alpha_1 > 0$  being a weighting parameter.

## The green agent's program

Therefore they solve the following maximization program:

$$\max_r m(r, p_t) + u(c_G(r))$$

$$\text{s.t.} \quad 0 \leq r \leq 1 \text{ and } q_t, p_t \text{ given.}$$

Hence the optimal level of contribution for the agent  $r^*(p_t)$  will be given by solving  $\frac{\partial U(r, p_t)}{\partial r} = 0$ .

# The Evolution of Society

Using the *replicator dynamics* we have that the growth rate of a trait is proportional to the pay-off's difference with respect to the population. Generally speaking:

$$\dot{q}_i = q_t(U_i - \bar{U})$$

(with  $\bar{U} = \sum_i q_i U_i$ )

In this case we have:  $\dot{q}_t = q_t(1 - q_t)(U_G - U_B)$

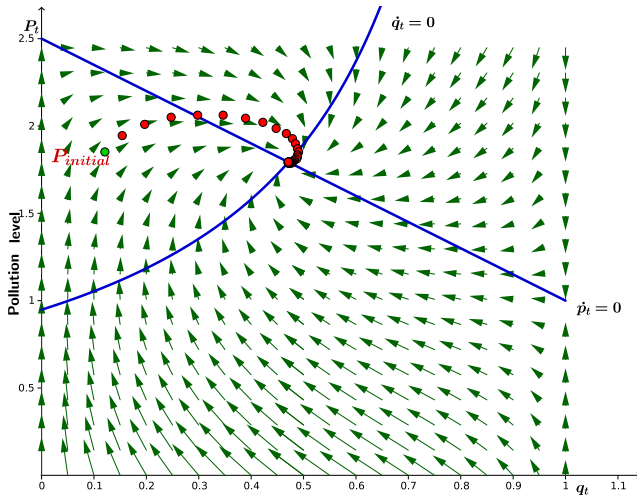
Where  $U_G - U_B = m(r^*, p_t) + \underbrace{u(c_G) - u(c_B)}_{\Delta_u: \text{the cost of being green}}$

(Depending on the functional form of  $u(c_i)$ ,  $\frac{\partial \Delta_u}{\partial w} \begin{matrix} \geq \\ < \end{matrix} 0$ )



# The Evolution of Society

$$\dot{p}_t = -\eta p_t + \gamma d_t \quad \text{and} \quad \dot{q}_t = q_t(1 - q_t)[m(r^*, p_t) + \Delta_u]$$



# The Evolution of Society

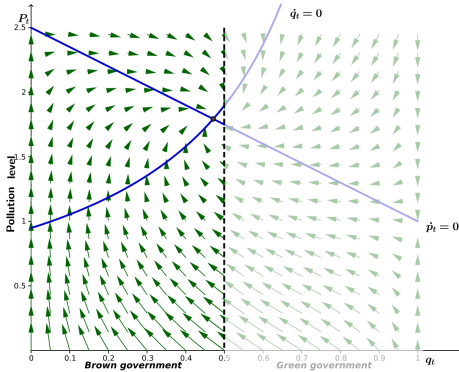
## The Governments:

- If  $q_t < 1/2$ , we will have a brown government: nothing will happen.
- If  $q_t \geq 1/2$ , we will have a green government, which will subsidize the green product.<sup>5</sup>
  - This will lower  $\rho$ .
  - Which in turn will change the dynamics equilibrium.

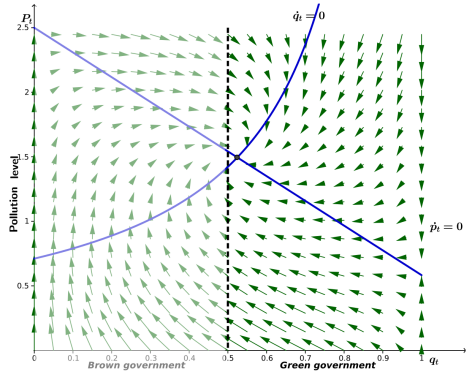
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<sup>5</sup>Or equivalently, it will tax the brown product.

# The Evolution of Society

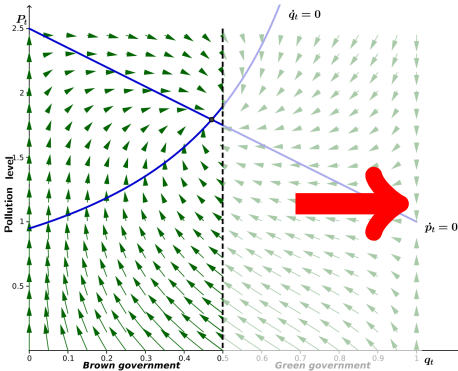


$q_t < 1/2 \rightarrow$  Brown government  
 $\rightarrow$  usual  $\rho$

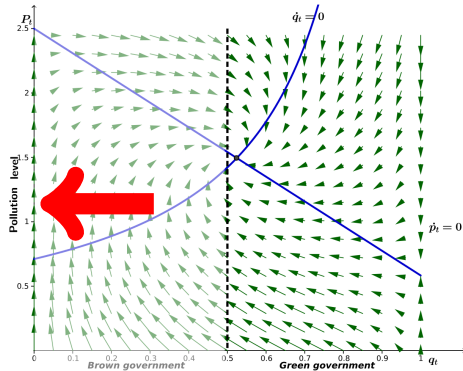


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# The Evolution of Society



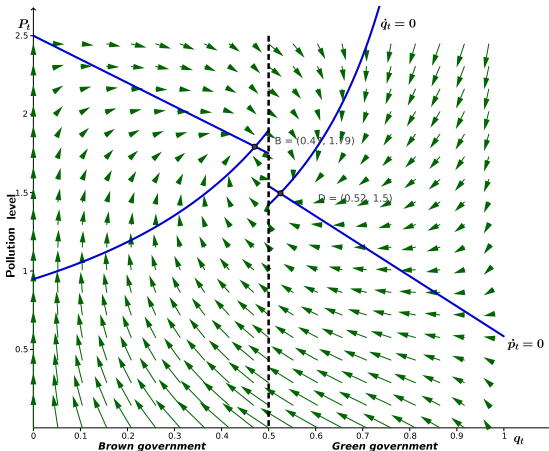
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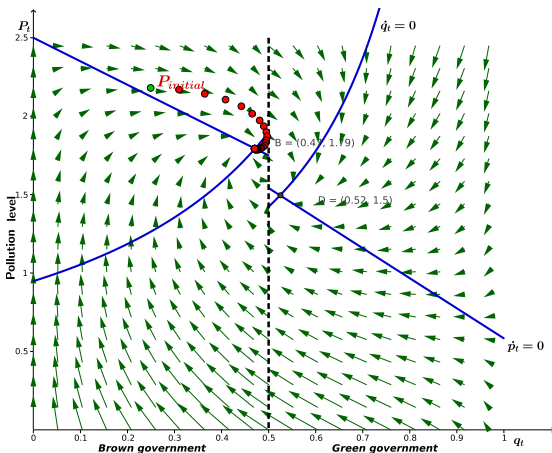
# Final Dynamics

- $\dot{p}_t = -\eta p_t + \gamma d_t$  and  $\dot{q}_t = q_t(1 - q_t)[m(r^*, p_t) + \Delta_u]$
- $\dot{q}_t = 0$  and  $\dot{p}_t = 0 \rightarrow \hat{p}_t(q_t)$  and  $\tilde{p}_t(q_t)$



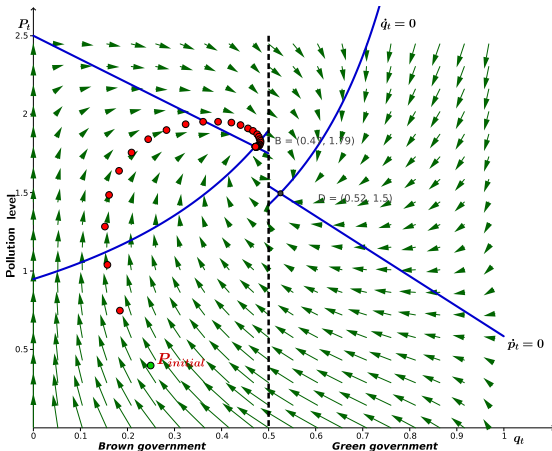
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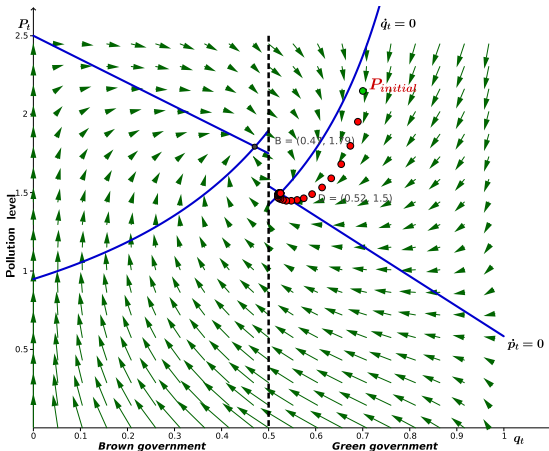
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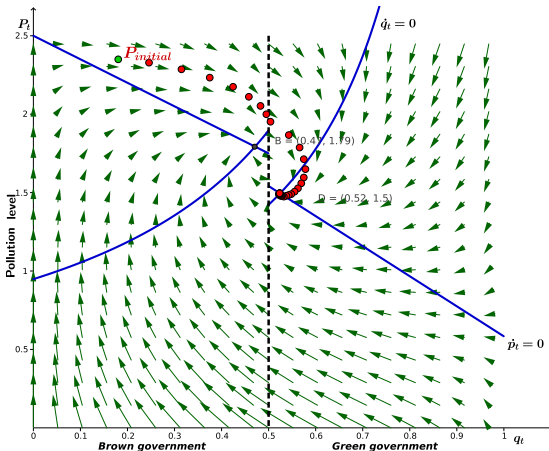
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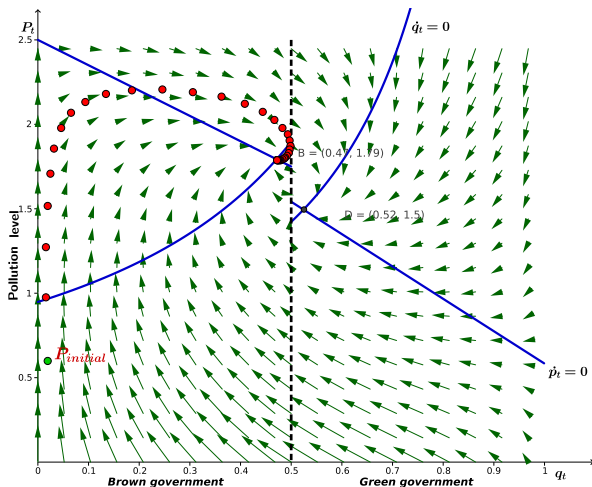


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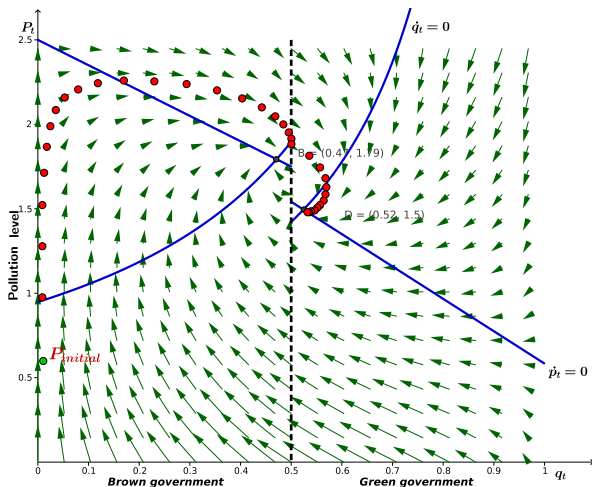


# Example of a limit trajectory



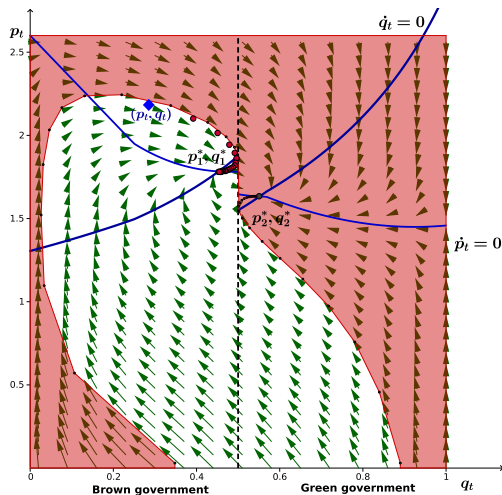
Example of a limit trajectory. Possibility of *tipping points*.

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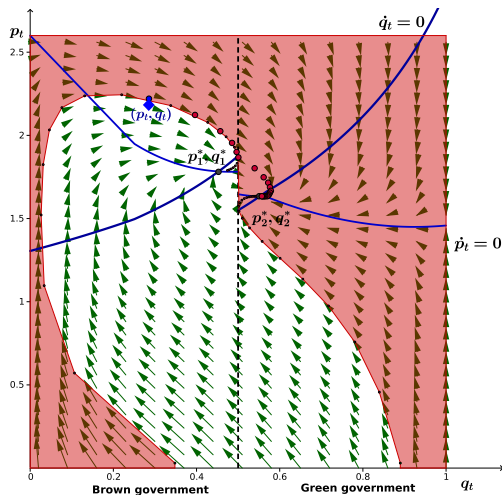
Example of a limit trajectory. Possibility of *tipping points*.

# Searching for an environmental nudge



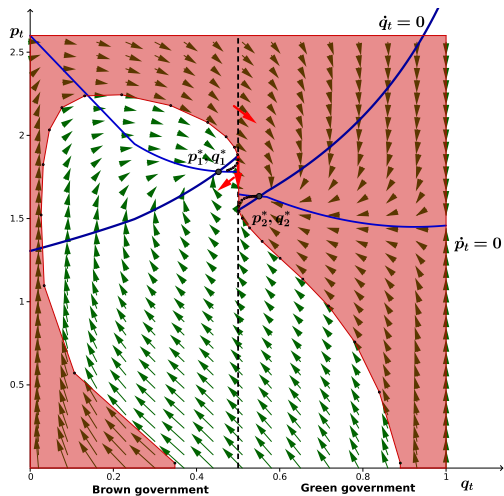
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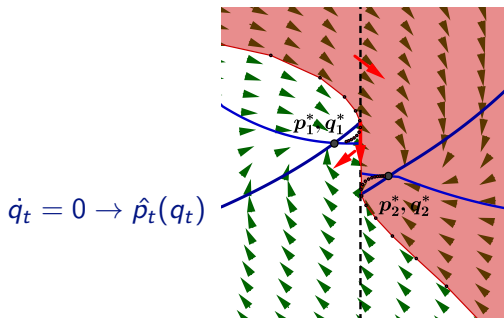


Example of a limit trajectory. Possibility of *tipping points*.

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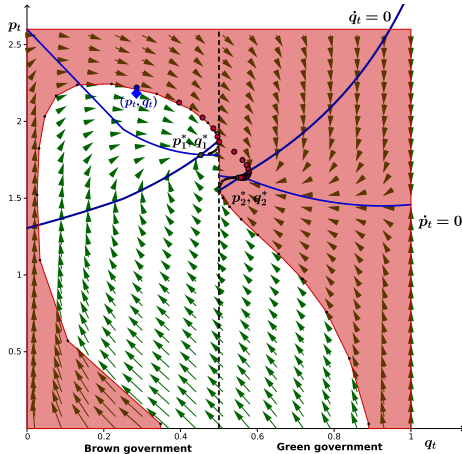
The limit trajectory can be 'defined' by

$$\lim_{q_t \rightarrow 1/2} \hat{p}_t(q_t)$$

And we can make sensibility analysis (work in progress):

How does it shift with  $\Omega_3$  (perception bias of the pollution level)?

# Searching for an environmental nudge



For example: A (temporary) change in  $\Omega_3$  could switch the system into the green path.



## Summing up - Conclusions

- The present model is compatible with the fact that we can have **similar countries behaving differently** with respect to the environment.
- Also people behave differently → possible explanation: a **moral motivation**.
- Using this idea, we can find a way to **switch** from a brown trajectory into a green one.
- Therefore we could find *where* to **nudge** in order to produce this change (work in progress).
- **Drawback:** It is difficult to measure some of these variables (real behaviour, motivation).

The End

Thank you

For your attention